#### PHYS127AL Lecture 8

David Stuart, UC Santa Barbara, October 19, 2021

More transistor circuits: Ebers-Moll, current mirror, differential amplifier, FETs



# Review: Transistor rules of operation

- 1).  $V_{BE} = 0.6 \text{ V}$  or the transistor is off I.e.,  $V_B = V_E + 0.6 \text{ V}$ Once the transistor is on,  $\Delta V_B = \Delta V_E$ .
- 2).  $I_C = \beta I_B$ . And by charge conservation  $I_E = I_B + I_C$  so  $I_E \cong I_C$

3).  $V_{CE} > 0.2 V$ 

With these simple rules we can analyze most transistor circuits. We'll add some nuance later today.





### Review: Constant current source

We can use a transistor to pull a *constant* specified current through a load.



To get a constant 1mA flow through  $R_L$ , even as  $R_L$  changes, we can set  $R_E$  to 1k and  $V_E$  to 1 V.

That sets the value of  $I_E$ , which is equal to  $I_C$ , regardless of  $R_L$ .

Choose  $R_1$  and  $R_2$  to make  $V_B = 1.6$  V. Then  $V_E = 1.0$  V.  $I_E = 1$  mA.  $I_C = 1$  mA, regardless of  $R_L$ .

This works until  $V_C < V_E + 0.2$ 

Note that there is no input signal here.

### Review: Constant current source

#### We can use this to pull a specified current through a load.

 $V_{CC} = +5 V$ R  $R_{\rm L}$  $R_{\rm E}$ VEE

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Choose the zener diode to make  $V_B = 1.6$  V. The zener reduces sensitivity to  $V_{CC}$  variations.



#### Constant current source

We can use a transistor to *pull* a *constant* specified current through a load. This is actually called a *current sink* since it pulls current from R<sub>L</sub>.



#### Constant current source

We can use a PNP transistor to *push* a *constant* specified current into a load.



Now we can switch the location of  $R_L$  and  $R_E$ . The base's bias voltage sets  $R_E$  which sets  $I_E$ and hence  $I_C$ .

For 1 mA we could set  $R_E = 1k$  and  $V_E = 4 V$ . That requires  $V_B = 3.4 V$  which we get from  $R_1 \& R_2$  choice.

 $3.4 = 5 R_2/(R_1 + R_2)$ 

## Ebers-Moll model

The simple transistor rules we have been using aren't the full picture. Two examples of features it misses.

Gain limit with R<sub>G</sub>=0.

I<sub>L</sub> is temperature dependent.



# Ebers-Moll model

Gain limit comes from intrinsic resistance in the transistor.



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$$I_C = I_s \left( e^{V_{BE}/nV_T} - 1 \right)$$

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A 2<sup>nd</sup> order correction incorporates effects from collector voltage differences

$$\begin{split} I_{\rm C} &= I_{\rm S} \left( e^{V_{\rm BE}/nV_{\rm T}} - 1 \right) \left( 1 + \frac{V_{\rm CE}}{V_{\rm AF}} \right) - I_{\rm S} \left( e^{V_{\rm BC}/nV_{\rm T}} - 1 \right) \left( 1 + \frac{V_{\rm CE}}{V_{\rm AR}} \right) - \frac{I_{\rm S}}{\beta_{\rm R}} \left( e^{V_{\rm BC}/nV_{\rm T}} - 1 \right) \\ I_{\rm B} &= \frac{I_{\rm S}}{\beta_{\rm F}} \left( e^{V_{\rm BE}/nV_{\rm T}} - 1 \right) - \frac{I_{\rm S}}{\beta_{\rm R}} \left( e^{V_{\rm BC}/nV_{\rm T}} - 1 \right). \end{split}$$

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We could amplify the signal before transmitting to make it large compared to any pickup. But then it becomes a powerful transmitter causing pickup on other wires nearby.



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Best to transmit signals with small signals that are immune to pickup; use low-voltage differential signals (LVDS) on twisted pairs of wires.





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Analyze this by 1<sup>st</sup> calculating V<sub>A</sub>.  

$$V_{A} = V_{EE} + I_{EE}R_{EE}$$

$$I_{EE} = I_{E1} + I_{E2}$$

$$= (V_{E1}-V_{A})/R_{E} + (V_{E2}-V_{A})/R_{E}$$

$$= (V_{E1}+V_{E2})/R_{E} - 2V_{A}/R_{E}$$

$$V_{A} = V_{EE} + R_{EE}/R_{E} (V_{E1}+V_{E2})/R_{E} - 2R_{EE}V_{A}/R_{E}$$

$$V_{A} = \frac{R_{E}V_{EE} + R_{EE} (V_{E1}+V_{E2})}{R_{E} + 2R_{EE}}$$

$$\Delta V_{A} = (\Delta V_{E1} + \Delta V_{E2}) \frac{R_{EE}}{R_{E} + 2R_{EE}}$$

$$If \Delta V_{E1} = -\Delta V_{E2} \text{ then } \Delta V_{A} = 0$$

This makes the right side just a common-emitter amp with  $v_{out} = (-R_C/R_E) v_2$ If  $v_2 = -\Delta V_{in}/2 = -v_{in}/2$  then  $v_{out} = (R_C/R_E)v_{in}/2$ .



Differential gain = 
$$R_C/2R_E$$

Analyze this by  $1^{st}$  calculating V<sub>A</sub>.  $V_A = V_{EE} + I_{EE}R_{EE}$  $\mathbf{I}_{\mathrm{EE}} = \mathbf{I}_{\mathrm{E1}} + \mathbf{I}_{\mathrm{E2}}$  $= (V_{E1}-V_A)/R_E + (V_{E2}-V_A)/R_E$  $= (V_{E1}+V_{E2})/R_E - 2V_A/R_E$  $V_{A} = V_{EE} + R_{EE}/R_{E} (V_{E1}+V_{E2})/R_{E} - 2R_{EE}V_{A}/R_{E}$  $V_{A} = \frac{R_{E}V_{EE} + R_{EE}\left(V_{E1}+V_{E2}\right)}{R_{E} + 2R_{EE}}$  $\Delta V_{A} = (\Delta V_{E1} + \Delta V_{E2}) \frac{R_{EE}}{R_{E} + 2R_{FF}}$ If  $\Delta V_{E1} = -\Delta V_{E2}$  then  $\Delta V_A = 0$ 

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Common mode gain =  $-R_C/(R_E+2R_{EE})$ Differential gain =  $R_C/2R_E$  Now consider the *common mode* signal, where  $v_1 = v_2 = \overline{v} = v_{CM}$ 

That makes  $\Delta I_{E1} = \Delta I_{E2} \& \Delta I_{EE} = 2\Delta I_{E1}$ 

Written with "variation notation" its  $i_{E1} = i_{E2}$  and  $i_{EE} = 2i_{E1}$ 

So,  $\Delta V_A = v_A = i_{EE}R_{EE} = 2i_{E1}R_{EE}$ Now use Ohm's law to find  $i_{E1}$  as  $i_{E1} = (v_E - v_A) / R_E$  $= (v_{CM} - 2i_{E1}R_{EE}) / R_E$ So,  $i_{E1} = v_{CM} / (R_E + 2R_{EE})$ 

 $v_{\text{out}} = -i_{\text{E1}} R_{\text{C}} = -v_{CM} R_{\text{C}} / (R_{\text{E}} + 2R_{\text{EE}})$ 



Get positive gain by selecting output from  $v_2 = -v/2$ 

Don't need output from other side, but we do need the other side to get the common mode suppression.

Comment on "CM" jargon.

To maximize the CMRR =  $G_{Diff}/G_{CM}$  make  $R_{EE}$  large.

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A current mirror makes R<sub>C</sub> large for differential signals and small for common mode.

So this circuit gives very maximal G<sub>Diff</sub> and a large common mode rejection ratio. But we no longer control the gain; we'll see how to do that separately later.

# Current limiter

Separate from having a constant current, we often want to limit I<I<sub>max</sub>.



If  $Q_2$ 's  $V_{BE}$ <0.6 V it turns off, so no current flows through  $R_b$  and  $Q_1$  has a high  $V_b$  and  $Q_1$  is on.

If enough current flows to cause the voltage drop across  $R_s$  to go above 0.6 V,  $Q_2$  turns on and current flows through  $R_b$ . That reduces the base voltage of  $Q_1$ , lowering the current through  $Q_1$ and hence the current through  $R_s$  to turn off  $Q_2$ . This rapid on/off leads to an equilibrium at the max current of 0.6/ $R_s$ .

I.e., attempts to increase the load current beyond  $I_L = 0.6/R_s$  (either by higher V<sub>CC</sub> or lower R<sub>L</sub>) will lead to a max current of  $0.6/R_s$ .

E.g.,  $R_S = 0.6\Omega$  limits load current to 1 A.













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Better to set the V<sub>out</sub> quiescent point at ground, with a dual power supply, and DC couple the output.

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Even better to use an emitter follower as the output stage.

Amplification done in a previous stage. This just drives the speaker.

 $R_E$  still needs to be small, with high power to  $V_{EE}$ .

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A diode does that, but temperature sensitive.

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A diode does that, but temperature sensitive. So use identical copies of the push-pull transistors. (Ebers-Moll)

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This is a junction FET (jFET) where a p-type region is implanted within an n-type bulk. The depletion region can be controlled by the gate. Lower  $V_g$  increases the depletion.

So changing the gate voltage controls n and I. Like pinching off a hose.



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drain

source

p-channel

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Electro-static discharge (ESD) is a risk for MOSFETs due to thin oxide.





